

ECON 337901

FINANCIAL ECONOMICS

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Consumer Optimization: The Risk Dimension

Do we really observe consumers trading in contingent claims?

Yes, if we think of financial assets as “bundles” of contingent claims.

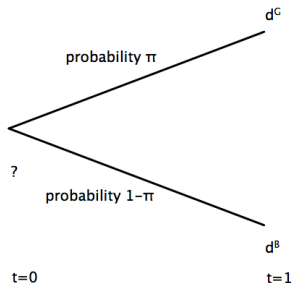
This insight is also Arrow and Debreu's.

Consumer Optimization: The Risk Dimension

A “stock” is a risky asset that pays dividend d^G next year in the good state and d^B next year in the bad state.

These payoffs can be replicated by buying d^G contingent claims for the good state and d^B contingent claims for the bad state.

Consumer Optimization: The Risk Dimension



Payoffs for the stock.

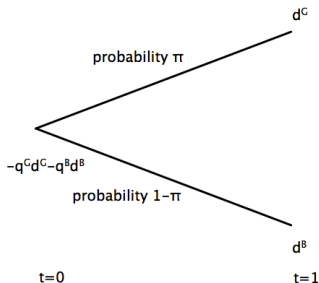
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If we start with knowledge of the contingent claims prices q^G and q^B , then we can infer that the stock must sell today for

$$q^{stock} = q^G d^G + q^B d^B.$$

Since if the stock cost more than the equivalent bundle of contingent claims, traders could make profits for sure by short selling the stock and buying the contingent claims; and if the stock cost less than the equivalent bundle of contingent claims, traders could make profits for sure by buying the stock and selling the contingent claims.

Consumer Optimization: The Risk Dimension



“Pricing” the stock.